Deformation Mapping for Coal Mining using Time-series InSAR Combining Persistent Scatterers and Distributed Scatterers in Huainan City, China

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1. INTRODUCTION

Underground coal mining often causes persistent land subsidence, which would lead to huge threats to infrastructure and safety in the coal area [1, 2]. Traditional levelling and GPS methods are able to produce reliable measurement of ground subsidence [3]. However, these field surveys are time-consuming and cannot provide deformation map with high spatial sampling density.

Synthetic aperture radar (SAR) interferometry (InSAR) is a powerful technology, which can obtain high precise elevation and surface deformation information along line of sight (LOS) using phase information from different SAR images. However, conventional InSAR usually suffers from temporal, geometrical and atmospheric decorrelation. In order to overcome these limitations, several advanced techniques have been proposed, such as Persistent Scatterer Interferometry (PSI) [4, 5] and Small baseline Subset Algorithm (SBAS) [6]. In recent years, Distributed Scatterers Interferometry (DSI) [7, 8] has been proposed to monitor the surface deformation with high spatial density of measurement points. The main drawback of DSI is the computational efficiency [7, 8] in large scale suburb areas.

This paper presents an approach to obtain ground deformation using time-series InSAR technique combining PSs and DSs. PSs are selected based on their coherence stability in the stack of interferograms. In order to identify DSs, a selecting strategy combining both classified information and statistical characteristics is used. To control the error propagation and improve the computational efficiency, deformation rate and DEM error on PSs are firstly retrieved using conventional PSI. Then a region grown-based strategy is applied to extract deformation rate on the useful DSs. A series of Radarsat-2 HH polarization images collected in Huainan are processed to verify the effectiveness of the proposed method. A dense ground surface deformation map is obtained. The experimental results show that the potential application of the proposed method.

2. METHOD

The block diagram of the proposed method is shown in Fig. 1. A selecting strategy combining both classified information and statistical characteristics is used to select DSs. Then the deformation parameters of PSs are retrieved using conventional PSI. Finally a region growing strategy is applied to extract deformation rates of DSs. In this study, we focus on two steps: selection of DSs and parameter estimation of DSs through a region growing method, which will be presented in this section.

2.1 Selection of DSs

DSs can be identified from the combination of classification analysis and mathematical statistics method. The former is to identify the specific classes for DSs, such as bare soil, ground and the sparse vegetation areas. The latter is to refine the candidates.

A DS object covers several pixels in high-resolution images, and these pixels are statistical homogeneous pixels (SHP) sharing the same behaviour corresponding to the suburban and soil area. However, water and forest area in the image are also homogeneous pixels, but not belonging to DSs. A prior classification map of the region can be of great help for DSs selection. In this paper, the classification map is generated by utilizing mean amplitude map of the SAR images to identify potential DSs classes.

For the collected candidates, an adaptive sample selection strategy is applied to refine them. Varies statistical tests have been proposed in recent years to identify homogenous pixels. The Anderson-Darling (AD) test has been proven to have better performance than Kolmogorov-Smirnov (KS) test [7]. Thus, AD test is adopted in this paper. For each candidate in the image, its statistical homogeneous pixels are identified, which can be applied to adaptive filtering as well as estimation of complex coherence value.
And then, those DS pixels are selected for further processing, which possess an average coherence greater than a certain threshold and have a minimum number of SHP.

Fig. 1 Block diagram of the proposed method.

2.2 Estimation Differential Deformation rate and DEM error between two points

Generally, the phase difference between two neighbouring pixels, \( x \) and \( y \), on each edge of network in the \( k \)th interferogram can be expressed as the following model:

\[
\Delta \phi^k_{\text{model}} = \frac{4\pi}{\lambda} T^k \cdot \Delta \nu^k_{(x,y)} + \frac{4\pi}{\lambda R \sin \theta} B^k \cdot \Delta \epsilon_{(x,y)}
\]

(1)

Where \( T^k \), \( B^k \), \( R \) and \( \theta \) denote time baseline, normal baseline, slant range, and incidence angle, respectively; \( \lambda \) is the wavelength and \( \Delta \nu \), \( \Delta \epsilon \) are the deformation rate variation and the elevation error variation of two neighbouring pixels.

The differential height error and deformation velocity are generated by maximizing the absolute value of \( \xi \),

\[
\xi = \frac{1}{N} \sum_{i=1}^{N} \exp \left( j \cdot (\Delta \phi^i_{\text{true}} - \Delta \phi^i_{\text{meas}}) \right)
\]

(2)

Where \( N \) is the number of interferograms, \( \Delta \phi^i_{\text{true}} \) is the phase difference of the neighbouring two points in the \( k \)th interferogram. The maximum of the absolute value of (2) is called temporal coherence.

2.3 Parameters estimation on PSs and DSs

In order to control the error propagation, deformation rate and topographic error on PSs are firstly retrieved using conventional PSI. After Delaunay network is constructed on PSs, the differential deformation rate and DEM error on each edge of the network are estimated using the method described in section 2.2. Once the estimation of deformation parameter of all edges on PSs has been done, the deformation velocity and DEM error of all the validate points can be obtained through integration step. After getting the linear deformation rate of PSs, the PSs with good quality are preserved and added into the processed target (PT) set. The valid deformation results from PS set are used as the reference data for parameters estimation of DS set.
Because of the large number of the DSs, it will be computationally expensive and difficult to retrieve deformation parameters if constructing Delaunay triangulation on DSs simultaneously. Therefore, a method using region growing strategy is applied to extract deformation rate and DEM error of DS set. Starting from a reference DS, all the DSs can be visited through a region growing method. For each DS, referring it as unprocessed target (UPT), neighbouring processed targets (PTs) from the PT set are identified using a selecting window (see Fig. 2). Then each of the PTs is linked with UPT and $\Delta v, \Delta e$ of the links are estimated using the method described in section 2.2. Only the link with temporal coherence large than a given threshold is viewed as validated link. If there is no validated links between UPT and PTs, the UPT is viewed as an invalid point. Otherwise, the LOS subsidence rate and elevation error of the UPT are obtained using (3) and (4) and the UPT is added into PT set:

$$V_c = \frac{\sum_{i=1}^{n_1} \xi_i \cdot (V_i + \Delta V_i)}{\sum_{i=1}^{n_1} \xi_i}$$ \hspace{1cm} (3)

$$E_c = \frac{\sum_{i=1}^{n_1} \xi_i \cdot (E_i + \Delta E_i)}{\sum_{i=1}^{n_1} \xi_i}$$ \hspace{1cm} (4)

Where $V_c, E_c$ are the estimated deformation rate and DEM error; $M$ is the number of the validated links; $v, e$ are the deformation rate and DEM error of the $i$th PT, respectively; $\Delta v, \Delta e, \xi$ denote the deformation rate, DEM error, and temporal coherence of the link between UPT and the $i$th PT, respectively. In the same way, all the UPT are analysed to retrieve the deformation rate and DEM error.

Once the linear deformation rate of all the points have been obtained, the nonlinear deformation components can be extracted using spatial and temporal filtering at both PSs and DSs.

![Fig. 2 Sketch of identifying processed targets](image)

3. STUDY AREA AND DATA

Huainan, located in the Yangtze River Delta hinterland central of Anhui province, is rich in coal resource, accounted for 19% of the national vision of stocks of coal stock. About 14 pairs of key state-owned coal mines are located in Huainan City. However, this anthropogenic activity has caused series land subsidence, which result in many series of environmental problems and damages. As shown in Fig. 3, the central part of Huainan is selected as the study area, in which there are five coal mining areas, Dingji, Guqiao, Zhangjiaji, Xinji I and Xinji II. In the coal mining areas, there are several collapsed lakes resulting from coal mining.
In order to monitor the subsidence of the coal mining area in Huainan city, 20 Radarsat-2 ascending images acquired from September 2012 to May 2014 with a look angle of 36.6 degrees and ‘HH’ polarization have been used (see Table 1). The SAR amplitude images (about $20 \times 20$ km$^2$) averaged from all the images for the study area is shown in Fig.3. The pixel spacing of range and azimuth is 2.66 m and 2.49 m, respectively. 97 interferometric pairs are combined to generate interferograms with perpendicular baseline less than 200 m and temporal baseline less than 200 days.

4. EXPERIMENTAL RESULT

After generating the average coherence map, point with coherence value large than 0.65 is selected as PS. 70939PSs are identified as shown in Fig. 4(A). The unsupervised IsoData method is used to generate the classification map based on the mean amplitude image. By removing the non-DSs classes, the DS candidates are obtained. Subsequently, AD test with a window of $11 \times 11$ is applied to select the DSs which have an average coherence larger than 0.45 and the number of SHP larger than 70. 1,142,592 DSs have been selected by the proposed selection strategy (approximately 2856 DSs/km$^2$), which is shown in Fig. 4(B). It is shown that the density of selected DSs is much higher than that of PSs in rural area.

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**Table 1 Radarsat-2 Data**

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Fig. 3 Location map of the study site and amplitude image. Five coal areas are marked. The two insets show the location of Anhui province in China and the coverage of a Radarsat-2 image.
Parameter estimation of DSs and collecting research will focus on parameter estimation of DSs. This paper has presented an approach to extract ground movement in coal mining area using time-series InSAR on PSs and DSs, thus resulting in more detail of the subsidence measurements. DSs can be efficiently identified using information and statistical property. A region growing strategy has been applied in the processing of DSs, which may make parameter estimation easier and more efficiency. Future work will focus on parameter estimation of DSs.

5. CONCLUSION

Experimental result on PSs is shown in Fig. 5. The average subsidence velocity of the study area is about 53.3 mm/year. It is shown that four subsidence areas are marked by red rectangle line with a peak subsidence rate of 107 mm/year. Those subsidence areas are located in the central of the coal mining area, which indicates that coal mining contribute to the ground movement. Future in-depth research will focus on parameter estimation of DSs and collecting ground truth data.

Fig.4 (A) selected PSs; (B) selected DSs

Fig.5 Subsidence velocity map on PSs.

This paper has presented an approach to extract ground movement in coal mining area using time-series InSAR on PSs and DSs, thus resulting in more detail of the subsidence measurements. DSs can be efficiently identified using information and statistical property. A region growing strategy has been applied in the processing of DSs, which may make parameter estimation easier and more efficiency. Future work will focus on parameter estimation of DSs.
ACKNOWLEDGMENTS

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6. REFERENCE